Spring 2006

## Homework 8 due June 2, 2006 in class

- **1.** Biggs 24.7.8 (pg. 356)
- 2. Biggs 24.7.12 (pg. 356)
- 3. Biggs 24.7.18 (pg. 356)
- 4. Biggs 25.3.5 (pg. 367)
- **5.** Biggs 26.1.3 (pg. 378)

6. For integers  $0 \le k \le n$ , the q-binomial coefficient is defined as

$$\binom{n}{k}_{q} = \frac{(q)_{n}}{(q)_{k}(q)_{n-k}}$$

where  $(q)_m = (1-q)(1-q^2)\cdots(1-q^m)$ . Show that  $\binom{n}{k}_q$  is the generating function of partitions with at most k parts and no part exceeding n-k.

[Hint: Show that

$$\binom{n}{k}_{q} = q^{k} \binom{n-1}{k}_{q} + \binom{n-1}{k-1}_{q}$$

and use induction.]