

1.) Solve the following differential equations.

a.) $\frac{dy}{dx} = xe^x$ b.) $\frac{dy}{dx} = xy\sqrt{y-4}$ c.) $\frac{dy}{dx} = \sin^3 x \cos^2 y$
 d.) $\frac{dy}{dx} = y^2(y-1)$ e.) $\frac{dy}{dx} = \sin x \cos y$ f.) $\frac{dy}{dx} = xy - y + 3x - 3$
 g.) $\frac{dy}{dx} = \frac{x + xy^3 + 1 + y^3}{xy^2 - 2y^2}$ h.) $\frac{dy}{dx} = e^{2x+3y}$ and $y(1) = 0$

2.) Let M be the total mass (in grams) of a black bullhead (a sport fish common throughout Minnesota's lakes with sandy, muddy bottoms) at time t (in years). Assume that its growth rate is given by $\frac{dM}{dt} = (1/100)M(400 - M)$. If $M(0) = 2$ grams, solve the D.E. and solve explicitly for mass M . What is the bullhead's mass in 1 year ? in 2 years ? Determine an upper limit (asymptotic mass) for the mass of this fish.

3.) Solve Problem B on page 2 of this discussion sheet.

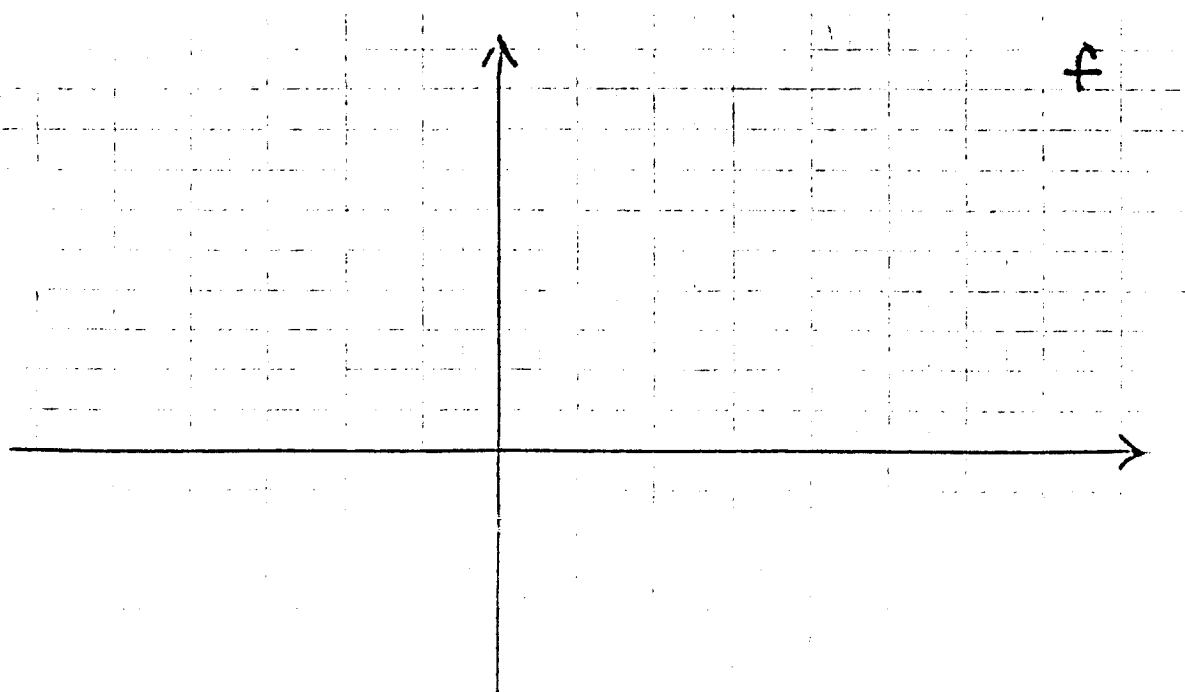
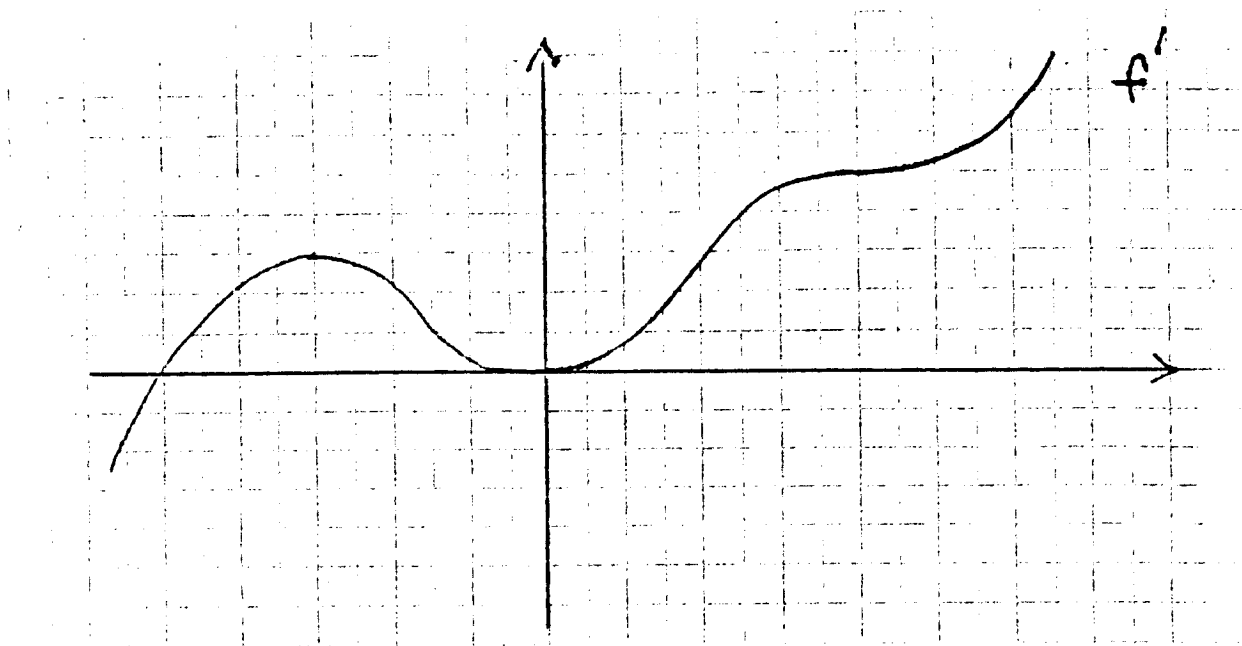
4.) Consider the function $f(x) = \cos 2x$ on the interval $[0, 1/2]$. What should n be in order that the Taylor Polynomial of degree n centered at $x = 0$ have a Taylor Error of at most 0.0001 ?

5.) Consider the function $f(x) = \frac{x}{x+1}$ on the interval $[0, 3/4]$. What should n be in order that the Taylor Polynomial of degree n centered at $x = 0$ have a Taylor Error of at most 0.0001 ?

THE FOLLOWING PROBLEM IS FOR RECREATIONAL PURPOSES ONLY.

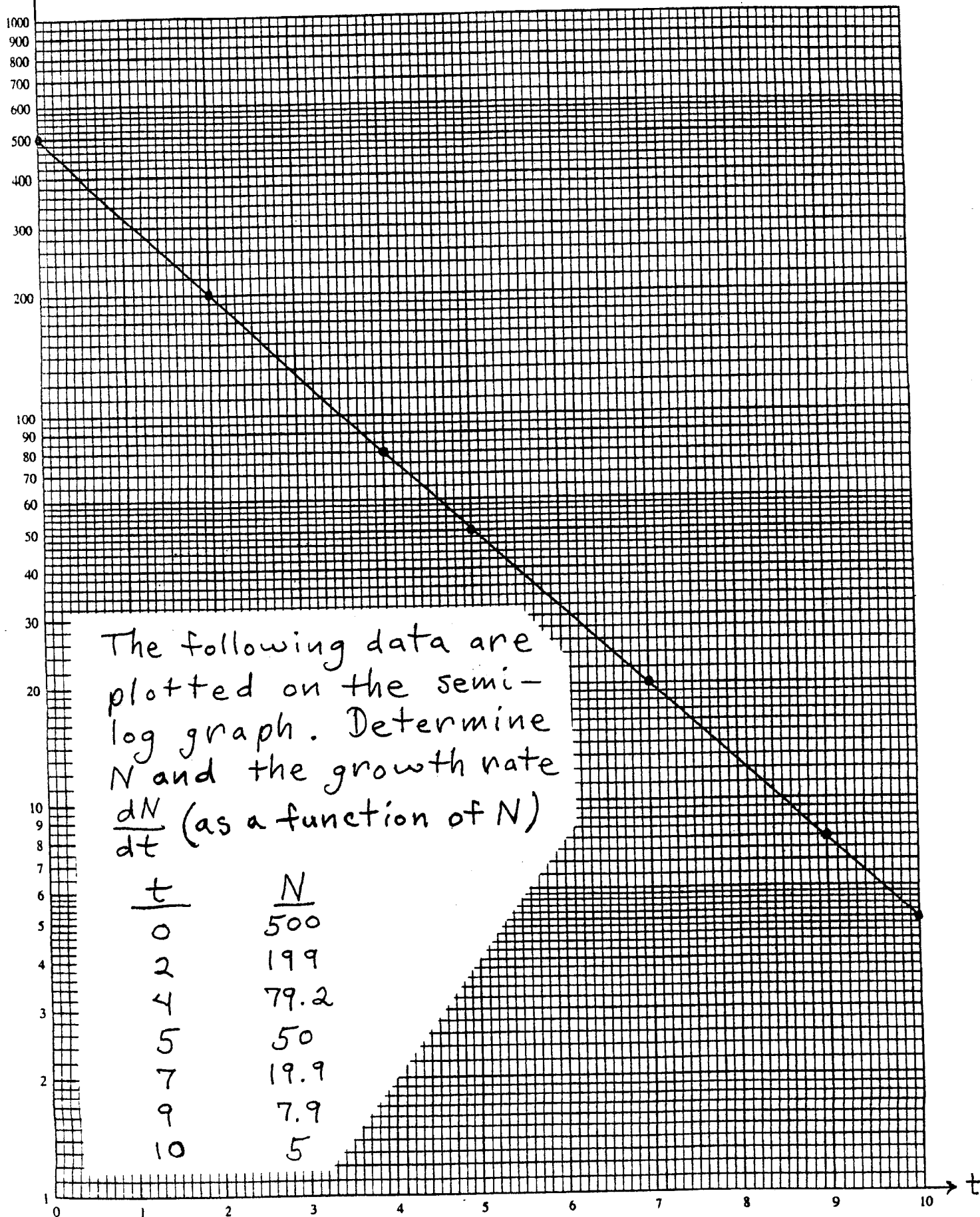
6.) You have 8 black socks, 12 blue socks, 10 gray socks, and 5 white socks randomly scattered in your bureau drawer. If you reach into the drawer without looking, how many socks must you take out to be sure of having a matching pair of socks ? a matching pair of white socks ?

- 1.) The graph of a derivative f' is given below. Set up a sign chart for the second derivative f'' and sketch a graph of the function f , indicating extrema and inflection points.



$\log N$

Problem B



Problem B (Solution)

Assume $\log N = \log C + rt$ (a line);
then $C = 500$ so $\log N = \log 500 + rt$,
and $t = 10, N = 5 \rightarrow$

$$\log 5 = \log 500 + 10r \rightarrow$$

$$\log 5 - \log 500 = 10r \rightarrow$$

$$\log \frac{5}{500} = 10r \rightarrow \log \frac{1}{100} = 10r \rightarrow$$

$$\log 10^{-2} = 10r \rightarrow -2 = 10r \rightarrow$$

$$r = -\frac{1}{5}; \text{ then}$$

$$\log N = \log 500 - \frac{1}{5}t \rightarrow$$

$$10^{\log N} = 10^{\log 500 - \frac{1}{5}t} \rightarrow$$

$$N = 10^{\log 500} \cdot 10^{-\frac{1}{5}t} \rightarrow$$

$$\boxed{N = 500 \cdot 10^{-\frac{1}{5}t}}; \text{ then}$$

$$\frac{dN}{dt} = \underbrace{500 \cdot 10^{-\frac{1}{5}t}}_N \cdot \ln 10 \cdot -\frac{1}{5} \rightarrow$$

$$\boxed{\frac{dN}{dt} = -\frac{\ln 10}{5} N}$$