

Math 21B

Kouba

Trig Identities and Antiderivatives

You need NOT memorize identities number 1.) through 4.).

$$1.) \sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$2.) \sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$3.) \cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$4.) \cos(A - B) = \cos A \cos B + \sin A \sin B$$

You MUST memorize the following identities and antiderivatives.

$$5.) \cos^2 x + \sin^2 x = 1$$

$$6.) \sin 2x = 2 \sin x \cos x$$

$$7.) \cos 2x = 2 \cos^2 x - 1 \quad \text{so that} \quad \cos^2 x = \frac{1 + \cos 2x}{2}$$

$$= 1 - 2 \sin^2 x \quad \text{so that} \quad \sin^2 x = \frac{1 - \cos 2x}{2}$$

$$= \cos^2 x - \sin^2 x$$

$$8.) 1 + \tan^2 x = \sec^2 x \quad \text{so that} \quad \tan^2 x = \sec^2 x - 1$$

$$9.) 1 + \cot^2 x = \csc^2 x \quad \text{so that} \quad \cot^2 x = \csc^2 x - 1$$

$$10.) \int \cos x \, dx = \sin x + C$$

$$20.) \int \frac{1}{1+x^2} \, dx = \arctan x + C$$

$$11.) \int \sin x \, dx = -\cos x + C$$

$$\text{and} \quad \int \frac{1}{a^2 + x^2} \, dx = \frac{1}{a} \arctan \frac{x}{a} + C$$

$$12.) \int \sec^2 x \, dx = \tan x + C$$

$$21.) \int \frac{1}{\sqrt{1-x^2}} \, dx = \arcsin x + C$$

$$13.) \int \csc^2 x \, dx = -\cot x + C$$

$$\text{and} \quad \int \frac{1}{\sqrt{a^2 - x^2}} \, dx = \arcsin \frac{x}{a} + C$$

$$14.) \int \sec x \tan x \, dx = \sec x + C$$

$$22.) \int \frac{1}{x\sqrt{x^2 - 1}} \, dx = \operatorname{arcsec}|x| + C$$

$$15.) \int \csc x \cot x \, dx = -\csc x + C$$

$$\text{and} \quad \int \frac{1}{x\sqrt{x^2 - a^2}} \, dx = \frac{1}{a} \operatorname{arcsec} \left| \frac{x}{a} \right| + C$$

$$16.) \int \tan x \, dx = \ln|\sec x| + C$$

$$17.) \int \cot x \, dx = \ln|\sin x| + C$$

$$18.) \int \sec x \, dx = \ln|\sec x + \tan x| + C$$

$$19.) \int \csc x \, dx = \ln|\csc x - \cot x| + C$$