Math 21C
Kouba
Discussion Sheet 7

1.) Compute the first five terms (starting with n=1) of each sequence. Determine whether each sequence converges or diverges.

a.) $\{3\}$ b.) $\{3^n\}$ c.) $\left\{\dfrac{3}{n}\right\}$ d.) $\left\{\left(\dfrac{1}{3}\right)^n\right\}$

e.) $\{3^{1/n}\}$ f.) $\left\{\dfrac{n+5}{n+2}\right\}$ g.) $\{n(3-n)\}$ h.) $\left\{\dfrac{n^3+n^2-n+7}{4n^3+5n^2-2}\right\}$

i.) $\{(0.9999)^n\}$ j.) $\{(1.00001)^n\}$ k.) $\left\{\left(\dfrac{-2}{3}\right)^n\right\}$ l.) $14/3, 15/5, 16/7, 17/9, ...$

m.) $\left\{\dfrac{\sin 3n}{n}\right\}$ n.) $\left\{\left(\dfrac{\sqrt{7}}{\ln 14}\right)^n\right\}$ o.) $\{\cos(2n\pi)\}$ p.) $\{(1+1/n)^n\}$

q.) $\left\{\dfrac{3^n}{n!}\right\}$ r.) $\{\sin(\pi/2+n\pi)\}$ s.) $\left\{\dfrac{1000^n}{n!}\right\}$ t.) $\left\{\dfrac{n^2}{e^n}\right\}$

u.) $\left\{(n-1)(n-2)(n-3)(n-4)(n-5)\right\}$ v.) $\{3+(-1)^n\}$ w.) $\left\{\displaystyle\sum_{i=1}^{n} i^2\right\}$

x.) $\left\{\displaystyle\sum_{i=1}^{n}(2/3)^{i-1}\right\}$ y.) $\left\{\displaystyle\sum_{i=1}^{n}(1+i/n)^3(1/n)\right\}$

2.) Determine whether the following series converge or diverge.

a.) $\displaystyle\sum_{n=1}^{\infty} 2^n$ b.) $\displaystyle\sum_{n=1}^{\infty} 2$ c.) $\displaystyle\sum_{n=1}^{\infty} \dfrac{1}{2^n}$ d.) $\displaystyle\sum_{n=1}^{\infty} 0.000001$

e.) $\displaystyle\sum_{n=1}^{\infty}(0.98)^{n+3}$ f.) $\displaystyle\sum_{n=1}^{\infty} 5(-2/3)^{n-1}$ g.) $\displaystyle\sum_{n=1}^{\infty}(-1)^n$ h.) $\displaystyle\sum_{n=1}^{\infty}(1/4)(3/2)^{n+3}$

i.) $\displaystyle\sum_{n=1}^{\infty} \dfrac{n+2}{n+1000}$ j.) $\displaystyle\sum_{n=1}^{\infty}(1-1/n)^n$ k.) $\displaystyle\sum_{n=1}^{\infty} \cos n\pi$

l.) $\displaystyle\sum_{n=1}^{\infty} \dfrac{1}{n^2+5n+6}$ HINT: Use partial fractions.

3.) Compute the exact value of the following convergent series :
$$6-2+\dfrac{2}{3}-\dfrac{2}{9}+\dfrac{2}{27}-\dfrac{2}{81}+...$$

4.) Find the 25th term in the following sequence : $1, 1, 2, 3, 5, 8, 13, 21, 34, ...$

5.) Find the sum of the first 200 terms in the following sequence : $3, 7, 11, 15, 19, 23, ...$

4.) A ball bearing is dropped from a building 200 feet high. Each time the ball bearing rebounds to 40% of its falling distance. What is the total distance the ball bearing will

travel ?

5.) Determine the limit of the following sequence :

$$2, \quad 2 - \frac{1}{2}, \quad 2 - \frac{1}{2 - \frac{1}{2}}, \quad 2 - \frac{1}{2 - \frac{1}{2 - \frac{1}{2}}}, \quad 2 - \frac{1}{2 - \frac{1}{2 - \frac{1}{2}}} \quad \ldots$$

6.) Start at the origin and move 10 units along the positive y-axis. Turn 90 degrees to the right and move 70% of that distance. Turn 90 degrees to the right and move 70% of that distance. Turn 90 degrees to the right and move 70% of that distance. Turn 90 degrees to the right and move 70% of that distance. Continue this process. At what point (x,y) will you "end" ?

"The mind is not a vessel to be filled, but a fire to be ignited." – Plutarch