## HOMEWORK 5

MATH 180, WINTER 2023
(1) Suppose $A$ and $B$ are two surfaces represented by polygonal decompositions. If the Euler characteristic of $A$ is $x$ and the Euler characteristic of $B$ is $y$, what is the Euler characteristic of their connected sum $A \# B$ in terms of $x$ and $y$ ?
(2) Use your formula from the previous question and induction to calculate the Euler characteristic of the connected sum of $g$ copies of the torus (i.e. the genus $g$ surface).
(3) Show that the two polygonal presentations below give homeomorphic surfaces.

(4) Show that the two polygonal presentations below give homeomorphic surfaces.

(5) Show that the two polygonal presentations below give homeomorphic surfaces.


