

**DEPARTMENT OF MATHEMATICS  
SYLLABUS**

Course # & Name: 258A Numerical Optimization

Recommended Text(s) & Price: 1. Nocedal/Wright, Numerical Optimization, 2<sup>nd</sup> edition, available for free on SpringerLink  
2. Boyd/Vandenberghe, Convex Optimization, available for free from Boyd's homepage

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Approval Date: \_\_\_\_\_

Prerequisites: 25 and 167, or consent of the instructor

<b>Lectures</b>	<b>Sections</b>	<b>Comments/Topics</b>
<b>0.5</b>	NW 1	Introduction
<b>0.5</b>	NW 2.1	Unconstrained optimization: Optimality conditions
<b>0.5</b>	NW 2.2, 3.1	Line search
<b>1.5</b>	NW 3.2—3.3	Convergence of line search. Linear convergence of steepest descent, local quadratic convergence of Newton.
<b>0.5</b>	BV 9.6	Self-concordant analysis of Newton.
<b>2.5</b>	NW 6.1—6.4 NW 7.2	Superlinear convergence of quasi-Newton methods. DFP, BFGS, Broyden, restricted Broyden, global convergence. Limited-memory BFGS (L-BFGS).
<b>3</b>	NW 12.1—12.7	Constrained optimization: First- and second order optimality conditions.
<b>1</b>	NW 12.9 BV 5.1—5.5	Lagrangian duality. Dual of convex quadratics.
<b>1</b>	BV 2.6, 4.4.2 BV 4.6, 5.9	Generalized inequalities: Conic, semidefinite, LMI. Their Lagrangean duality.
<b>1.5</b>	NW 16.1—16.5	Active-set methods for convex quadratic optimization.
<b>1</b>	NW 18.1—18.4	Sequential quadratic programming
<b>1</b>	NW 17.1—17.3	Penalty functions
<b>0.5</b>	NW 15.4, 18.3	Merit functions
<b>1.5</b>	NW 14.1—14.2	Primal-dual path-following interior point methods for linear optimization
<b>1</b>	NW 19.1—19.5	Interior point algorithms for general nonlinear optimization problems; line search vs. trust region
<b>2</b>	*	Application: Compressive sensing. Conditions for the equivalence of $l_0$ and $l_1$ optimization. Numerical aspects, such as the LASSO algorithm and/or $l_1$ minimization via interior point methods.



## Additional Notes:

The indicated number of lectures refers to 80-minute lectures.

The syllabus accounts for 19.5 of 20 lectures of one quarter. Recommended are take-home midterms or individual/group projects rather than in-class midterms.

\* Source for compressed sensing: the paper

<http://www.acm.caltech.edu/~emmanuel/papers/RIP.pdf>

and probably some more sources