

# 115 Homework 4

Due Friday October 29

**Question 1** Definition: if  $p$  is prime and  $p^a|n$  while  $p^{a+1} \nmid n$  we say that  $p^a$  divides  $n$  *exactly* and write  $p||n$ . (Rosen 3.4.12) Show that  $p^a||m \Rightarrow p^{ka}||m^k$ .

**Question 2** (Rosen 3.4.17,18) Find all  $n \in \mathbb{N}$  such that  $n!$  ends with 74 zeros (in base ten). Show  $n!$  never ends with 153, 154 or 155 zeros.

**Question 3** (Rosen 3.5.4 a,c,e) Use Fermat's method to factor 8051, 46009 and 3,200,399.

**Question 4** (Rosen 3.5.20) Find all primes  $2^{2^n} + 5$  where  $n + 1 \in \mathbb{N}$ .

**Question 5** (Rosen 3.6.14) A piggy bank contains \$2 made from 24 coins which are nickels, dimes and quarters. What combinations of coins are possible?