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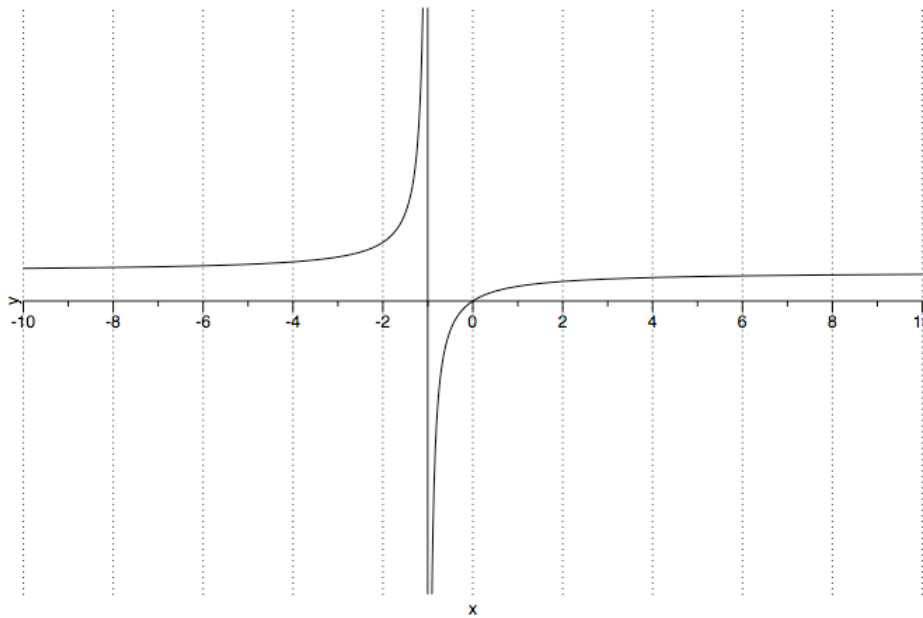
Correction from lecture:

23.) Find the values of  $x \in \mathfrak{R}$  for which the given function is continuous:

$$f(x) = \ln\left(\frac{x}{x+1}\right)$$

$\ln(x)$  is continuous on  $(0, \infty)$ . The domain of  $g(x) = \frac{x}{x+1}$  is  $\{x \in \mathfrak{R} \mid x \neq -1\}$ . Let's see

what the range of  $g(x) = \frac{x}{x+1}$  is:



The range of  $g(x)$  is positive from  $(-\infty, -1) \cup (0, \infty)$ . Therefore  $f(x) = \ln(g(x))$  is defined there, and  $f(x)$  is continuous on  $(-\infty, -1) \cup (0, \infty)$ .