- 1. Solve. Write your answers in interval notation.
 - (a.) $4b-5 \ge b+1$ and 7b+4 > 9b-6
 - (b.) Same as part (a), except with "or" instead of "and": $4b-5 \ge b+1$ or 7b+4 > 9b-6
 - (c.) $5|q-2|-7 \le 8$
- 2. Consider the function $f(x) = \begin{cases} -x+3 & \text{if } x < 1, \\ -|x-5|+6 & \text{if } 1 \le x < 9. \end{cases}$
 - (a.) Sketch a graph of y = f(x) by transforming functions that you know. Be sure to label your axes. Include and label any intercepts.
 - (b.) Find the domain of f(x). Write your answer in interval notation.
 - (c.) Find the range of f(x). Write your answer in interval notation.
- 3. Find the domain of each function. Write your answers in interval notation.

(a.)
$$f(x) = \ln \left[\frac{2x - x^2}{x^2 + 4x - 5} \right]$$

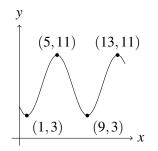
(b.) $g(x) = \sqrt{\frac{x+1}{x-2} - \frac{x+2}{x+3}}$

4. Consider the graph of
$$y = \frac{2(x-1)^2(x+3)}{(x+2)^2(x-4)} = \frac{2x^3 + 2x^2 - 10x + 6}{x^3 - 12x - 16}$$
.

- (a.) Find all *x* and *y*-intercepts.
- (b.) Find all horizontal and vertical asymptotes.
- (c.) Sketch a graph. Be sure to label your axes. Include and label any intercepts, asymptotes, and holes.

5. Consider the graph of
$$y = \frac{x(x-3)(x-1)}{(x-3)(x+3)} = \frac{x^3 - 4x^2 + 3x}{x^2 - 9}$$
.

- (a.) Find the x- AND y-coordinates of any holes.
- (b.) Find all horizontal, vertical, and slant (oblique) asymptotes.
- 6. Find an equation for the graph below. Write your answer in the form $y = A\sin(Bx + C) + D$ OR $y = A\cos(Bx + C) + D$.



- 7. Sketch each graph. Draw and label axes, asymptotes, and intercepts.
 - (a.) $y = 3^{x-2} 4$
 - (b.) $y = 2\ln(x+3) 4$
- 8. Sketch each graph. Include **at least** two periods. Draw and label axes, asymptotes, and intercepts. Clearly show the coordinates of all local maxima and minima.

(a.)
$$y = 7\csc(3\pi x)$$

(b.) $y = 5\cot(x/3)$
(c.) $y = -2\cos\left(3x - \frac{\pi}{2}\right)$
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- 9. Suppose $\sin \theta = -\frac{3}{5}$ and angle θ measures between π and $3\pi/2$. Find the exact value of $\sin\left(\frac{\theta}{2}\right)$, $\cos\left(\frac{\theta}{2}\right)$, and $\tan\left(\frac{\theta}{2}\right)$.
- 10. Simplify each expression as much as possible. Remember to think about domains and ranges!

(a.)
$$\arccos\left[\sin\left(-\frac{\pi}{3}\right)\right]$$

(b.) $\cot\left[\arccos\left(-\frac{1}{2}\right)\right]$
(c.) $\tan\left[\arccos\left(\frac{5}{2x}\right)\right]$
Hint: Draw a right triangle.

11. Find ALL real solutions to each equation.

(a.)
$$4\sin x = 2\sqrt{3}$$

(b.)
$$5\cos x = -2$$

$$(c.) \cos x - \sin x = \frac{\sqrt{2}}{2}$$

- 12. Verify the identity $\frac{\csc x}{\cot x + \tan x} = \cos x$. Remember to start with one side of the equation, then change it step-by-step to the other side. Tell me whether each step is ALGEBRA or a TRIG IDENTITY.
- 13. (a.) Simplify $\begin{pmatrix} 30\\ 26 \end{pmatrix}$. Your final answer should be a product of integers, e.g., $4 \cdot 7 \cdot 8$.
 - (b.) Find the coefficient of n^4m^5 when $(3n+m)^9$ is expanded. You may leave your answer in terms of factorials.