

## Homework 5

due Wednesday February 12 in class

This is a short homework! The midterm will be held February 12 in class. I posted a practice midterm exam; the solution will be discussed in the discussion session on February 11.

**1. Biggs 13.7 # 3** page 288

Show that if  $H$  and  $K$  are subgroups of  $G$  then so is  $H \cap K$ .

**2. Biggs 13.10 # 13** page 298

Let  $H$  and  $K$  be subgroups of a finite group  $G$  such that  $\gcd(|H|, |K|) =$

1. Show that  $|H \cap K| = 1$ .

**3. Biggs 13.10 # 5** page 297

Show that if  $H$  is a subgroup of index 2 in a group  $G$  then the left coset  $gH$  is the same as the right coset  $Hg$  for all  $g \in G$ .