## Advanced Linear Algebra. Syllabus

| L \# | Topics | Notes \& Remarks |
| ---: | :--- | :--- |
| 1 | What is Linear Algebra? | Notes |
| 2 | Complex Numbers | Notes |
| 3 | Complex Numbers |  |
| 4 | Fundamental Theorem of Algebra (proof optional) | Notes |
| 5 | Vector Spaces, Subspaces | Axler pp 4-14 |
| 6 | Direct Sum, Span | Axler pp 14-23 |
| 7 | Linear Independence, Bases | Axler pp 23-31 |
| 8 | Dimension | Axler pp 31-34 |
| 9 | Linear Maps | Axler p 37-41 |
| 10 | Null Space, Range | Axler pp 41-47 |
| 11 | Matrix of a Linear Map | Axler pp 48-53 |
| 12 | More on Matrices | Notes |
| 13 | Invertibility | Axler pp $53-58$ |
| 14 | Eigenvalues and eigenvectors | Axler pp 75-80 |
| 15 | Existence of Eigenvalues | Axler pp 81-84 |
| 16 | Upper Triangular Matrix Representation | Axler pp 84-90 |
| 17 | Diagonalization (2x2) and Applications | Notes |
| 18 | Midterm |  |
| 19 | Inner Product Spaces | Axler pp $97-101$ |
| 20 | Cauchy-Schwarz, Triangle Inequality, Pythagoras | Axler pp 101-106 |
| 21 | Orthonormal Bases, Gram-Schmidt procedure | Axler pp 106-110 |
| 22 | Orthogonal Projections, Minimization Problems | Axler pp 111-116 |
| 23 | Vectors and Coordinates - Maps and Matrices | Notes |
| 24 | Spectral Theorem for Normal Maps (complex) | Axler pp 127-133 |
| 25 | Diagonalization | Notes |
| 26 | Positive Operators, Polar and Singular Value Decomposition | Axler pp 144-155 |
| 27 | Permutations and the Determinant | Notes |
| 28 | Properties of the Determinant | Notes |
| 29 | LU-Factorization and Solving Linear Systems | Notes |

Notes of all lectures are available on the class website at http://www.math.ucdavis.edu/~anne/WQ2007/mat67.html

Additional handouts with useful material are:
Common Math Symbols, Notes on Sets and Functions, Matrices, Solving Linear Equations, Homework Sets and Solutions

