

Math 21C (Spring 2006)
Kouba
Exam 3

PRACTICE EXAM

Please PRINT your name here :

Your Exam ID Number

1. PLEASE DO NOT TURN THIS PAGE UNTIL TOLD TO DO SO.
2. IT IS A VIOLATION OF THE UNIVERSITY HONOR CODE TO, IN ANY WAY, ASSIST ANOTHER PERSON IN THE COMPLETION OF THIS EXAM. COPYING ANSWERS FROM ANOTHER STUDENT'S EXAM IS A VIOLATION OF THE UNIVERSITY HONOR CODE. PLEASE KEEP YOUR OWN WORK COVERED UP AS MUCH AS POSSIBLE DURING THE EXAM SO THAT OTHERS WILL NOT BE TEMPTED OR DISTRACTED. THANK YOU FOR YOUR COOPERATION.
3. YOU MAY USE A CALCULATOR ON THIS EXAM.
4. No notes, books, or classmates may be used as resources for this exam.
5. Read directions to each problem carefully. Show all work for full credit. In most cases, a correct answer with no supporting work will receive LITTLE or NO credit. What you write down and how you write it are the most important means of your getting a good score on this exam. Neatness and organization are also important.
6. You have until 5:00 p.m. sharp to finish the exam. PLEASE STOP WRITING IMMEDIATELY when time is called and close your exam.
7. Make sure that you have 7 pages including the cover page.

1.) (9 pts.) Let $z = 3x + \ln(x^2 + y)$. Compute the partial derivatives z_x , z_y , and z_{xx} . DO NOT SIMPLIFY your answers.

2.) Consider the surface given by $z = xy + y^3 - x^2$ and the point $(2, 1)$.

a.) (6 pts.) What is the maximum possible value of $D_{\vec{u}}f(2, 1)$ and in what direction is it ?

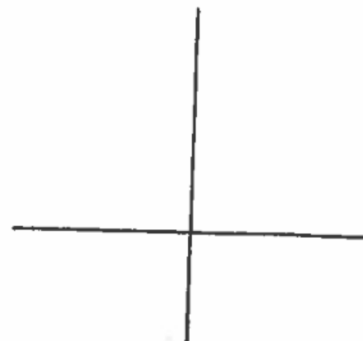
b.) (3 pts.) What is the minimum possible value of $D_{\vec{u}}f(2, 1)$ and in what direction is it ?

3.) (9 pts.) Evaluate the following limit : $\lim_{(x,y) \rightarrow (1,-1)} \frac{1 - \sqrt{x+y+1}}{x+y}$

4.) (9 pts.) Verify that the following limit does not exist : $\lim_{(x,y) \rightarrow (0,0)} \frac{xy^3}{x^2 + y^6}$

5.) Let $f(x, y) = 4 - \sqrt{y - x^2}$.

a.) (5 pts.) Determine and sketch the domain of f in 2D-space.



b.) (5 pts.) State the range of f . BRIEFLY explain how you get your answer.

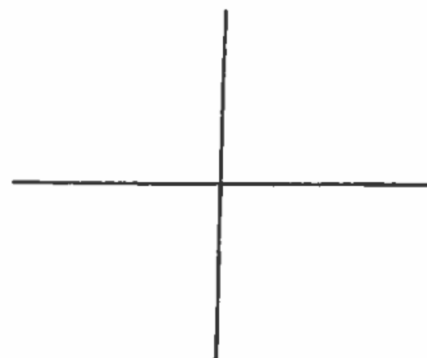
6.) (9 pts.) Use the Chain Rule to find and simplify (as much as possible) the second-order partial derivative $\frac{\partial^2 z}{\partial s^2}$, where $z = f(x, y)$, $x = 3r + s^2$, and $y = rs$.

- 7.) Consider the function given by $z = x^2 + y^2 - 4$ and its graph in 3D-space.
a.) (4 pts.) Determine all possible intercepts for this equation.

- b.) (4 pts.) Determine and sketch the xy -trace, xz -trace, and yz -trace.



- c.) (4 pts.) Sketch level curves on the same axes for $z = -3, 0$, and 5 .



- d.) (4 pts.) Sketch the surface in 3D-space.