

Example : Integrate .

$$1.) \int \cos x \cdot \sin^3 x \, dx \quad (\text{Let } u = \sin x \\ \xrightarrow{D} du = \cos x \, dx)$$

$$= \int u^3 \, du = \frac{1}{4} u^4 + C = \frac{1}{4} (\sin x)^4 + C$$

$$2.) \int (\cos 2x + \sec^2 x) \, dx$$

$$= \frac{1}{2} \sin 2x + \tan x + C$$

$$3.) \int (\sec x \tan x + \underline{\tan^2 x}) \, dx$$

$$= \int (\sec x \tan x + (\sec^2 x - 1)) \, dx$$

$$= \sec x + \tan x - x + C$$

$$4.) \int (\sin 3x - \cos 3x)^2 \, dx$$

$$= \int (\underline{\sin^2 3x} - 2 \sin 3x \cos 3x + \underline{\cos^2 3x}) \, dx$$

$$= \int (1 - 2 \sin 3x \cos 3x) \, dx$$

$$= x - 2 \int \sin 3x \cos 3x \, dx$$

$$\quad \quad \quad \uparrow \quad (\text{Let } u = \sin 3x \xrightarrow{D} \dots)$$

$$= x - \frac{1}{3} \sin^2 3x + C$$