

Face-to-Face with an Indefinite Integral

methods

examples

1.) formula

$$\int e^x dx = e^x + c$$

$$\int \frac{1}{x} dx = \ln|x| + c$$

2.) algebra

$$\int \tan x dx = \ln|\sec x| + c$$

a.) separate fraction

$$\int \frac{x^3+1}{x^2} dx$$

b.) +, - same term

$$\int \frac{x}{x+1} dx$$

c.) square term

$$\int x(x^3+1)^2 dx$$

d.) polynomial division

$$\int \frac{x^3}{x+1} dx$$

3.) chain rule backwards

$$\int x^2 e^{x^3} dx$$

$$\int \sec^2 x (1 + \tan x)^5 dx$$

4.) u-substitution

a.) standard

$$\int x^2 e^{x^3} dx, \int \frac{e^x}{1+e^x} dx$$

b.) u-sub., solve for x

$$\int (x+1)\sqrt{x+2} dx$$

c.) obscure u-sub.

$$\int \frac{\sqrt{x}}{1+\sqrt{x}} dx$$

5.) integration by parts: $\int u dv = uv - \int v du$

a.) standard

$$\int x e^x dx, \int \ln x dx$$

b.) more than once

$$\int x^2 \sin x dx$$

c.) obscure

$$\int \frac{x^3 e^{x^2}}{(x^2+1)^2} dx$$

6.) partial fractions

a.) standard

$$\int \frac{1}{x^2-4} dx = \int \left[\frac{\frac{1}{4}}{x-2} + \frac{-\frac{1}{4}}{x+2} \right] dx$$

b.) repeated factors

$$\int \frac{1}{x^3-x^2} dx = \int \left[\frac{-1}{x} + \frac{-1}{x^2} + \frac{1}{x-1} \right] dx$$

c.) divide first

$$\int \frac{x^4}{(x-1)^3} dx$$