

Section 10.3

$$1.) f(x, y) = x^2 y + x y^2 \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = 2xy + y^2 \text{ and } \frac{\partial f}{\partial y} = x^2 + x \cdot 2y$$

$$3.) f(x, y) = (xy)^{3/2} - (xy)^{2/3} \rightarrow$$

$$\frac{\partial f}{\partial x} = \frac{3}{2} (xy)^{1/2} \cdot y - \frac{2}{3} (xy)^{-1/3} \cdot y \text{ and}$$

$$\frac{\partial f}{\partial y} = \frac{3}{2} (xy)^{1/2} \cdot x - \frac{2}{3} (xy)^{-1/3} \cdot x$$

$$6.) f(x, y) = \tan(x - 2y) \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = \sec^2(x - 2y) \cdot (1) \text{ and } \frac{\partial f}{\partial y} = \sec^2(x - 2y) \cdot (-2)$$

$$7.) f(x, y) = \cos^2(x^2 - 2y) \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = 2 \cos(x^2 - 2y) \cdot -\sin(x^2 - 2y) \cdot 2x \text{ and}$$

$$\frac{\partial f}{\partial y} = 2 \cos(x^2 - 2y) \cdot -\sin(x^2 - 2y) \cdot (-2)$$

$$9.) f(x, y) = e^{\sqrt{x+y}} \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = e^{\sqrt{x+y}} \cdot \frac{1}{2} (x+y)^{-1/2} \cdot (1) \text{ and}$$

$$\frac{\partial f}{\partial y} = e^{\sqrt{x+y}} \cdot \frac{1}{2} (x+y)^{-1/2} \cdot (1)$$

$$10.) f(x, y) = x^2 e^{-\frac{1}{2}xy} \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = x^2 \cdot e^{-\frac{1}{2}xy} \cdot \left(-\frac{1}{2}y\right) + 2x \cdot e^{-\frac{1}{2}xy} \text{ and}$$

$$\frac{\partial f}{\partial y} = x^2 \cdot e^{-\frac{1}{2}xy} \cdot \left(-\frac{1}{2}x\right)$$

$$13.) f(x, y) = \ln(2x + y) \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = \frac{1}{2x+y} \cdot (2) \text{ and } \frac{\partial f}{\partial y} = \frac{1}{2x+y} \cdot (1)$$

$$17.) f(x, y) = 3x^2 - y - 2y^2 \xrightarrow{D}$$

$$f_x = 6x \text{ so } f_x(1, 0) = 6(1) = 6$$

$$19.) g(x, y) = e^{x+3y} \xrightarrow{D}$$

$$g_y = e^{x+3y} \cdot (3) \text{ so } g_y(2, 1) = 3e^{2+3(1)} = 3e^5$$

$$22.) g(v, w) = \frac{w^2}{v+w} \xrightarrow{D}$$

$$g_v = \frac{(v+w)(0) - w^2(1)}{(v+w)^2} = \frac{-w^2}{(v+w)^2} \text{ so}$$

$$g_v(1, 1) = \frac{-(1)^2}{(1+1)^2} = -\frac{1}{4}$$

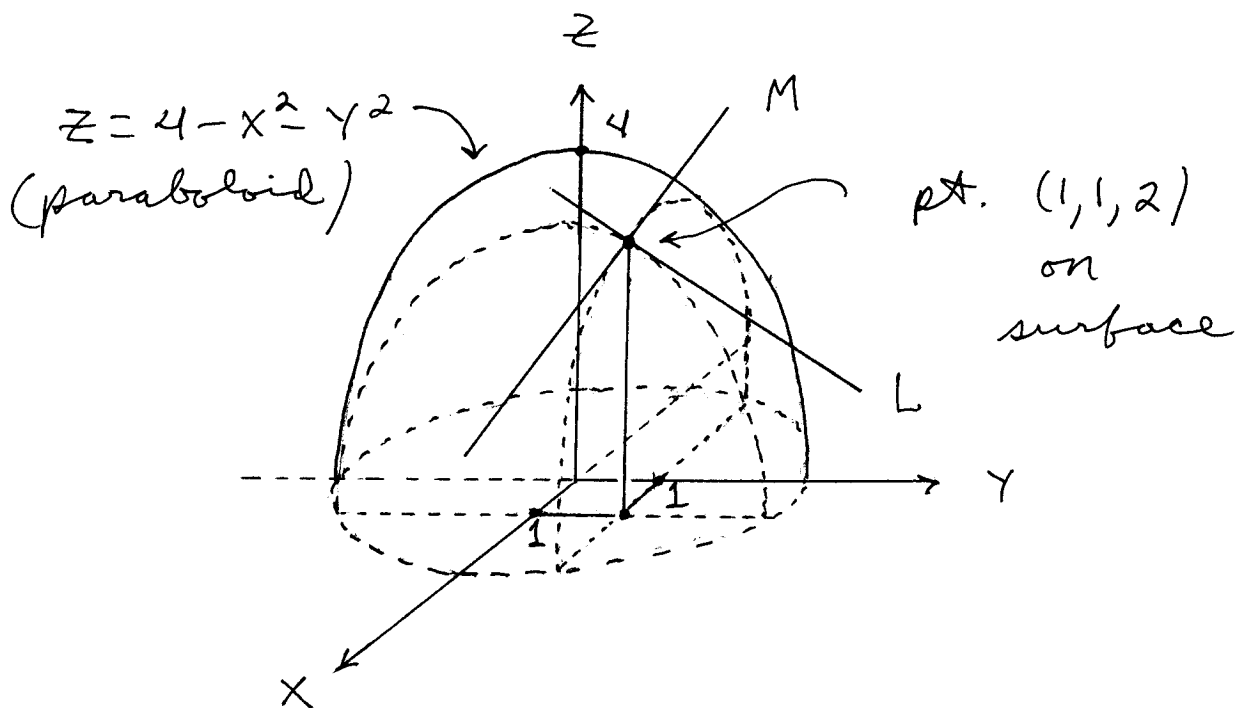
$$23.) f(x, y) = \frac{xy}{x^2+2} \xrightarrow{D}$$

$$f_x = \frac{(x^2+2)y - xy \cdot (2x)}{(x^2+2)^2} \text{ so}$$

$$f_x(-1, 2) = \frac{(1+2)(2) - (-2)(-2)}{(1+2)^2} = \frac{2}{9}$$

$$25.) f(x, y) = 4 - x^2 - y^2 \xrightarrow{D}$$

$$f_x = -2x \text{ and } f_y = -2y \text{ so}$$



$f_x(1,1) = -2$ is slope of line M
(tangent to surface in positive
x-direction) ; and
 $f_y(1,1) = -2$ is slope of line L
(tangent to surface in positive
y-direction)

30.) Per capita growth rate

$$f(P, H) = \frac{1}{H} \frac{dH}{dt} = r \left(1 - \frac{H}{K}\right) - aP$$

b.) If $P \uparrow$, then $\frac{\partial f}{\partial P} = -a$ so
per capita growth rate is $\downarrow$.

a.) If $H \uparrow$, then $\frac{\partial f}{\partial H} = r \cdot \left(\frac{-1}{K}\right) = -\frac{r}{K}$ so
per capita growth rate is $\downarrow$.

$$39.) f(x, y) = x^2 y + x y^2 \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = 2xy + y^2 \xrightarrow{D} \frac{\partial^2 f}{\partial x^2} = 2y$$

$$40.) f(x, y) = xy^2 - 3y^3 \xrightarrow{D}$$

$$\frac{\partial f}{\partial y} = 2xy - 9y^2 \xrightarrow{D} \frac{\partial^2 f}{\partial y^2} = 2x - 18y$$

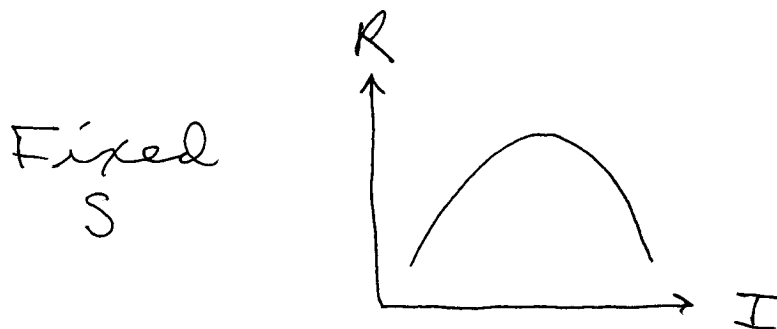
$$41.) f(x, y) = x e^y \xrightarrow{D}$$

$$\frac{\partial f}{\partial y} = x e^y \xrightarrow{D} \frac{\partial^2 f}{\partial x \partial y} = e^y$$

$$42.) f(x, y) = \sin(x - y) \xrightarrow{D}$$

$$\frac{\partial f}{\partial x} = \cos(x - y) \cdot (1) \xrightarrow{D} \frac{\partial^2 f}{\partial y \partial x} = -\sin(x - y) \cdot (-1)$$

51.) Let R : Crop Growth Rate,
 I : Leaf Area Index,
 S : Percent of Full Sunlight



Fixed
 I

