

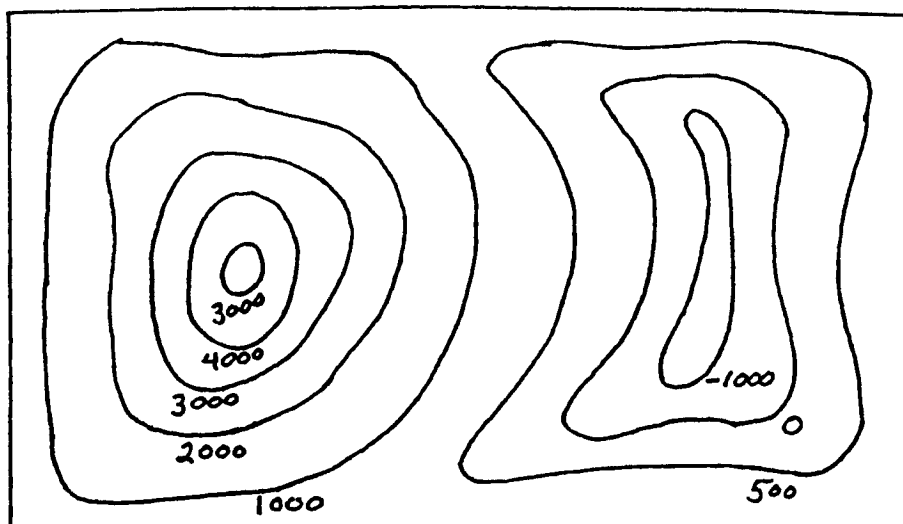
Math 17C

Kouba

# Sketching Surfaces in 3D-Space Using Level Curves and Traces

## RECALL : Topographical Map

Assume that the numbers represent height in feet relative to sea level of a particular region.

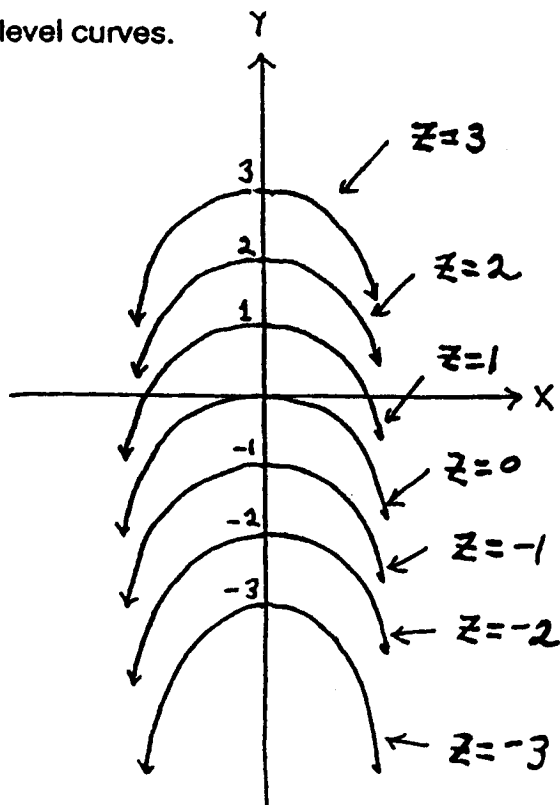


**DEFINITION** : The intersection of a horizontal plane at a particular height  $z = c$  with a given surface is called a level curve.

**EXAMPLE** : Sketch the surface  $z = x^2 + y$  using level curves.

Values for  $z$       Level curves

-3	$-3 = x^2 + y$	$y = -x^2 - 3$
-2	$-2 = x^2 + y$	$y = -x^2 - 2$
-1	$-1 = x^2 + y$	$y = -x^2 - 1$
0	$0 = x^2 + y$	$y = -x^2$
1	$1 = x^2 + y$	$y = -x^2 + 1$
2	$2 = x^2 + y$	$y = -x^2 + 2$
3	$3 = x^2 + y$	$y = -x^2 + 3$



DEFINITION : The intersection of each coordinate plane (xy-plane ( $z=0$ ), xz-plane ( $y=0$ ), and yz-plane ( $x=0$ )) with a given surface is called a trace.

EXAMPLE : Sketch the traces (on separate coordinate axes) for the surface  $z = x^2 + y$ .

$x=0$  : (yz-trace)

$y=0$  : (xz-trace)

$z=0$  : (xy-trace)

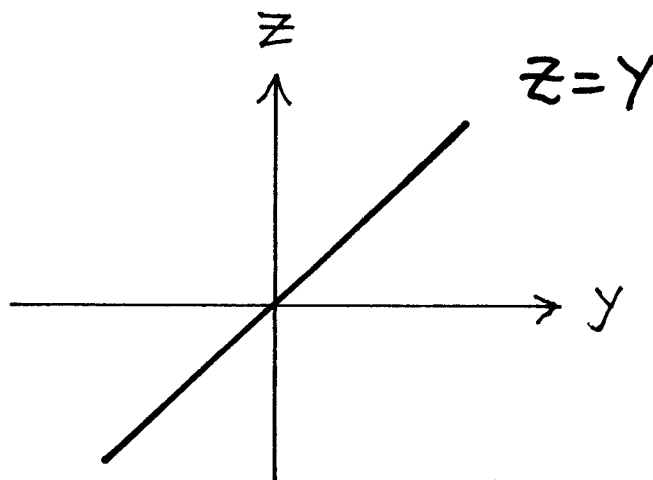
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EXAMPLE : Sketch the traces (on separate coordinate axes) for the surface  $z = x^2 + y$ .

$x=0$  : (yz-trace)

$$z = y$$

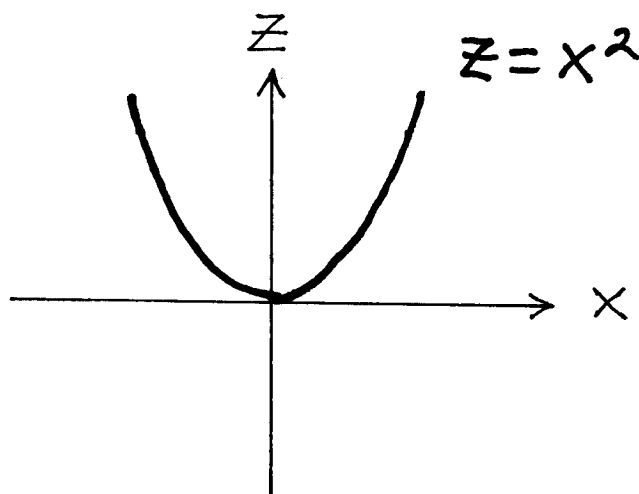
(line)



$y=0$  : (xz-trace)

$$z = x^2$$

(parabola)



$z=0$  : (xy-trace)

$$0 = x^2 + y$$

$$\rightarrow y = -x^2$$

(parabola)

