

KEY

Please PRINT your name here : _____

Your Four-Digit Exam ID Number _____

1. IT IS A VIOLATION OF THE UNIVERSITY HONOR CODE TO, IN ANY WAY, ASSIST ANOTHER PERSON IN THE COMPLETION OF THIS QUIZ. IT IS A VIOLATION OF THE UNIVERSITY HONOR CODE TO COPY ANSWERS FROM ANOTHER STUDENT'S EXAM. PLEASE KEEP YOUR OWN WORK COVERED UP AS MUCH AS POSSIBLE DURING THE QUIZ SO THAT OTHERS WILL NOT BE TEMPTED OR DISTRACTED. THANK YOU FOR YOUR COOPERATION. VIOLATIONS CAN RESULT IN EXPULSION FROM THE UNIVERSITY.

2. No notes, books, or classmates may be used as resources for this exam. YOU MAY USE A CALCULATOR ON THIS EXAM.

3. Read directions to each problem carefully. Show all work for full credit. In most cases, a correct answer with no supporting work will receive little or no credit. What you write down and how you write it are the most important means of your getting a good score on this quiz. Neatness and organization are also important.

4. Make sure that you have 3 pages, including the cover page.

5. You may NOT use L'Hopital's Rule on this exam.

6. You may NOT use any shortcuts for finding limits to infinity.

7. Using only a calculator to determine limits will receive little or no credit.

8. You will be graded on proper use of limit notation.

1.) (12 pts.) Let $f(x) = \begin{cases} \frac{x^2 - 7x + 6}{x - 6}, & \text{if } x \neq 6 \\ 4, & \text{if } x = 6. \end{cases}$. Show that f is NOT continuous at $x = 6$.

i.) $f(6) = 4$

ii.) $\lim_{x \rightarrow 6} \frac{x^2 - 7x + 6}{x - 6} = \lim_{x \rightarrow 6} \frac{(x-6)(x-1)}{x-6}$
 $= \lim_{x \rightarrow 6} (x-1) = 5$

iii.) But $\lim_{x \rightarrow 6} f(x) = 5 \neq 4 = f(6)$

so f is NOT continuous at $x = 6$.

2.) (13 pts.) USE LIMITS to determine all vertical and horizontal asymptotes for $y = \frac{3x-2}{x-1}$.

$$\lim_{x \rightarrow \pm\infty} \frac{3x-2}{x-1} \cdot \frac{\frac{1}{x}}{\frac{1}{x}} = \lim_{x \rightarrow \pm\infty} \frac{3 - \frac{2}{x}}{1 - \frac{1}{x}}$$

$$= \frac{3-0}{1-0} = 3 \quad \text{so} \quad \boxed{\text{H.A. : } y = 3};$$

$$\lim_{x \rightarrow 1^+} \frac{3x-2}{x-1} = \frac{\text{"1"}}{0^+} = +\infty \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{so}$$

$$\lim_{x \rightarrow 1^-} \frac{3x-2}{x-1} = \frac{\text{"1"}}{0^-} = -\infty \quad \left. \begin{array}{l} \\ \end{array} \right\} \boxed{\text{V.A. : } x = 1}$$

3.) (15 pts.) Use the Intermediate Value Theorem (IMVT) to prove that the following equation is solvable : $x^3 = 3x + 5$

$x^3 - 3x - 5 = 0$ so let $f(x) = x^3 - 3x - 5$
and let $m = 0$; f is continuous
for all x -values since it is a
polynomial; note that $f(0) = -5$
and $f(3) = 13$ and $m = 0$ is between
these values; use the interval
 $[0, 3]$; by the IMVT it
follows that there is at
least one number c , $0 \leq c \leq 3$,
so that $f(c) = m$, i.e.,

$c^3 - 3c - 5 = 0$, and
the original equation is
solvable.