

CSE 680 - Problem Set 2

Due beginning of lecture on October 26th

Problem numbers are from the second edition or the third of “Introduction to algorithms”. If unsure about which problem to solve, ask. Collaboration is permitted; looking for solutions from external sources (books, the web, etc.) is prohibited.

1. 2.3-7, 4.3-2, 4.4-6, 4.4-8. (Equivalently, 2.3-7, 4.1-1, 4.2-2, 4.2-4, from the second edition of book)
2. Give the asymptotic running time of the following algorithms in Θ notation. Justify your solution.

(a)

```
function func1(n)
  s = 0
  for i = 2*n to n^2 do
    for j = i to n^2 do
      s = s + j - i
    endfor
  endfor
  return(s)
```

```
(b) function func2(n)
    s = 0
    for i = 1 to n^2 do
        j = i^3
        while j > 10 do
            j = floor(j/5)
            s = s + j - i
        endwhile
    endfor
    return(s)
```

3. Write a recurrence relation describing the worst case running time of each of the following algorithms and determine the asymptotic complexity of the function defined by the recurrence relation. Justify your solution. Assume that all arithmetic operations take constant time.

```
(a) function func3(n)
    if n <= 10 then return(n)
    x = floor(n/7)
    x = x + func3(floor(3n/4))
    return(x)
```

```
(b) function func4(A,n)
    /* A is an array of n integers */
    if n <= 2 then return (A[1])
    for i = 1 to floor(n/2) do
        A[i] = A[i] + A[i+1]
        B[i] = A[i] - A[i-1]
        C[i] = A[i] + A[2*i]
    endfor
    x = 0
    x = x + func4(A, floor(n/3))
    x = x + func4(B, floor(n/3))
    x = x + func4(C, floor(n/3))
    return(x)
```