

Give the asymptotic running time of each the following functions in Θ notation. Justify your answer. (Show your work.)

1.

```

Func1(n)
1 s  $\leftarrow 0;$ 
2 for i  $\leftarrow 23$  to  $\lfloor n^{3/2} \rfloor$  do
3   for j  $\leftarrow 15$  to  $i^2 \lfloor (\log_5(i))^2 \rfloor$  do
4     | s  $\leftarrow s + i - j;$ 
5   | end
6 end
7 return (s);
```

2.

```

Func2(n)
1 s  $\leftarrow 0;$ 
2 for i  $\leftarrow \lfloor n/2 \rfloor$  to  $\lfloor n \log_4(n) \rfloor$  do
3   for j  $\leftarrow i$  to  $\lfloor n \log_4(n) \rfloor$  do
4     for k  $\leftarrow 3j$  to  $3j + 216$  do
5       | s  $\leftarrow s + i - j + k;$ 
6     | end
7   | end
8 end
9 return (s);
```

3.

```

Func3(n)
1 s  $\leftarrow 0;$ 
2 for i  $\leftarrow 7n^2$  to  $n^3$  do
3   | j  $\leftarrow \lfloor \sqrt{i} \rfloor;$ 
4   | while (j  $\geq 4$ ) do
5     |   | s  $\leftarrow s + i - j;$ 
6     |   | j  $\leftarrow j - 17;$            /* Note: Subtraction */
7   | end
8 end
9 return (s);
```

4.

```

Func4(n)
1 s  $\leftarrow 0;$ 
2 for i  $\leftarrow \lfloor n/2 \rfloor$  to  $\lfloor n^{3/2} \rfloor$  do
3   for j  $\leftarrow \lfloor n/10 \rfloor$  to i do
4     | for k  $\leftarrow j$  to i do
5       |   | s  $\leftarrow s + i - j + k;$ 
6     |   | end
7   | end
8 end
9 return (s);
```

5.

```

Func5(n)
1 s  $\leftarrow 0;$ 
2 i  $\leftarrow 29;$ 
3 while (i <  $n^2$ ) do
4   | j  $\leftarrow 6;$ 
5   | while j  $\leq 5n^3$  do
6   |   | s  $\leftarrow s + i - j;$ 
7   |   | j  $\leftarrow 3 * j;$ 
8   |   end
9   |   i  $\leftarrow i + \lceil 5\sqrt{n} \rceil;$            /* Note: Addition */
10  end
11 return (s);

```

6.

```

Func6(n)
1 s  $\leftarrow 0;$ 
2 i  $\leftarrow n;$ 
3 while (i <  $\lfloor n^3\sqrt{n} \rfloor$ ) do
4   | j  $\leftarrow 4;$ 
5   | while (j <  $3i$ ) do
6   |   | s  $\leftarrow s + i - j;$ 
7   |   | j  $\leftarrow j + 17;$            /* Note: Addition */
8   |   end
9   |   i  $\leftarrow 5 * i;$            /* Note: Multiplication */
10  end
11 return (s);

```

7.

```

Func7(n)
1 s  $\leftarrow 0;$ 
2 for i  $\leftarrow 3$  to  $\lfloor n \log_3(n) \rfloor$  do
3   | j  $\leftarrow i^2;$ 
4   | while (j >  $\lceil \sqrt{i} \rceil$ ) do
5   |   | s  $\leftarrow s + i - j;$ 
6   |   | j  $\leftarrow \lfloor j/7 \rfloor;$            /* Note: Division */
7   |   end
8 end
9 return (s);

```

8.

```

Func8(n)
1 s  $\leftarrow 0;$ 
2 i  $\leftarrow \lfloor n \log_9(n) \rfloor;$ 
3 while (i > 23) do
4   | /* Note: Division by i */           /*
5   | for j  $\leftarrow 62$  to  $\lfloor n^2 \log_7(n)/i \rfloor$  do
6   |   | s  $\leftarrow s + i - j;$ 
7   |   end                               /* Note: Division */
8   |   i  $\leftarrow \lfloor i/3 \rfloor;$ 
9 end
9 return (s);

```

9.

```
    Func9(n)
1  s ← 0;
2  i ← ⌊√n⌋;
3 while (i > 3) do
4   | j ← 5;
5   | while (j < n4) do
6   |   | s ← s + i - j;
7   |   | j ← (1.1) * j ;           /* Note: Multiplication */
8   | end
9   | i ← ⌊i/12⌋ ;                /* Note: Division */
10 end
11 return (s);
```

10.

```
    Func10(n)
1  s ← 0;
2  i ← 25;
3 while (i < n3) do
4   | j ← 6;
5   | while (j < i2) do
6   |   | s ← s + i - j;
7   |   | j ← j + ⌊√i⌋ ;          /* Note: Addition */
8   | end
9   | i ← 7 * i ;                /* Note: Multiplication */
10 end
11 return (s);
```