

# CSE 725 - Problem Set 3

## Due lecture on March 10th

Problem numbers are from the second edition of Sipser's book. If unsure about which problem to solve, ask. Collaboration is permitted; looking for solutions from external sources (books, the web, etc.) is prohibited. As a warmup, solve but do not turn in 7.21.

1. 7.17
2. 7.24
3. \* 7.27 (Optional hint: do not follow the hint in the book and show  $\neq SAT \leq_P 3COLOR$ , where  $\neq SAT$  is from problem 2.)
4. Show that  $2COLOR \in P$ , where

$2COLOR = \{\langle G \rangle : \text{the nodes of } G \text{ can be colored with two colors such that no two nodes joined by an edge have the same color}\}.$

5. (extra credit) \* Show that if  $P = NP$ , then  $EXP = NEXP$ , where

$$EXP = \bigcup_{k \geq 1} TIME(2^{n^k}),$$
$$NEXP = \bigcup_{k \geq 1} NTIME(2^{n^k}).$$