

① Find  $\int \frac{1}{x^3 + 4x^2} dx$ .

② Find  $\int e^{4x} \sin 2x dx$ .

③ Find  $\int \frac{3x^4 - 4x - 12}{x^3 - 2x^2} dx$ .

④ Evaluate  $\int_1^{\sqrt{e}} \frac{\ln x}{x^3} dx$ .

⑤ Evaluate  $\int_{1/4}^{\infty} \frac{15}{2x^2 + 5x + 2} dx$ , or show that it diverges.

⑥ Find  $\int \cos \sqrt{x} dx$ .

⑦ The time  $T$  (in hours) to recover after a race is a random variable with PDF  $f(t) = \frac{1}{2\sqrt{2t+1}}$ ,  $[0, 4]$ .

A) Find the probability that a person will take less than 90 min. to recover.

B) Find the expected recovery time.

⑧ The length of the parabola  $y = x^2$  from  $(0, 0)$  to  $(4, 16)$  is given by  $S = \int_0^4 \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx = \int_0^4 \sqrt{1 + 4x^2} dx$ .

Approximate this length using  $n = 4$  and

a) the trapezoidal rule.

b) Simpson's rule.

⑨ Evaluate  $\int_0^{\infty} \frac{1}{x + \sqrt{x}} dx$ , or show that it diverges.