

5. Evaluate

$$\int \frac{1}{x^3} \sqrt{\frac{x^2-1}{x^2}} dx.$$

$$\int \frac{1}{x^3} \sqrt{\frac{x^2-1}{x^2}} dx$$

$$= \int \sqrt{1 - \frac{1}{x^2}} \cdot \frac{1}{2} d\left(1 - \frac{1}{x^2}\right)$$

$$= \frac{1}{2} \cdot \frac{2}{3} \left(1 - \frac{1}{x^2}\right)^{\frac{3}{2}} = \frac{1}{3} \left(1 - \frac{1}{x^2}\right)^{\frac{3}{2}}$$

6. Evaluate

$$\int_{-1}^1 (x^2 - 2x + 1) dx.$$

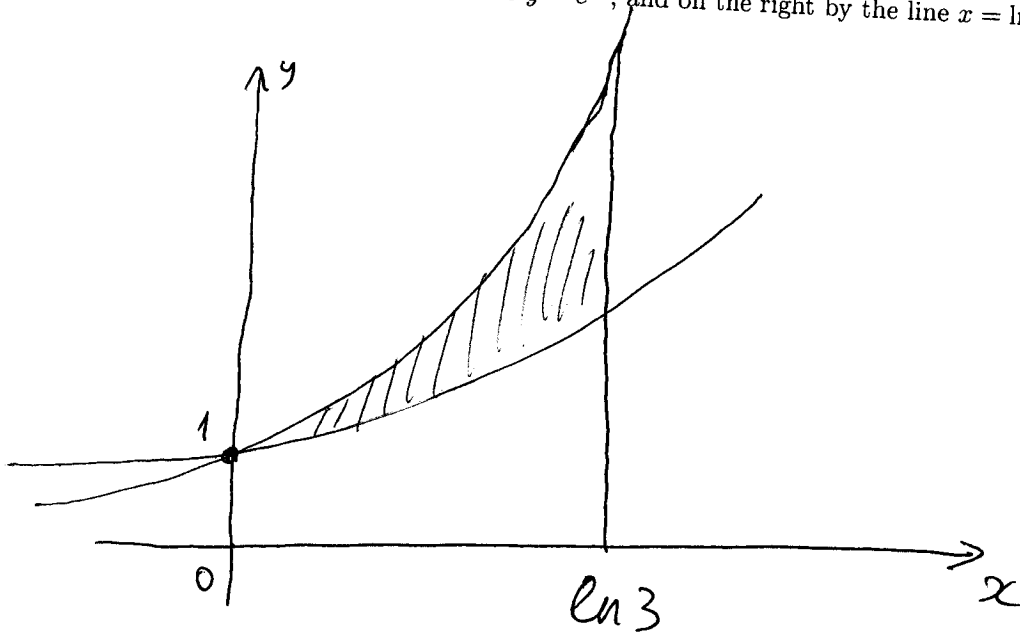
$$\int_{-1}^1 (x^2 - 2x + 1) dx$$

$$= \left. \frac{x^3}{3} - x^2 + x \right|_{-1}^1$$

$$= \left(\frac{1}{3} - 1 + 1 \right) - \left(-\frac{1}{3} - 1 - 1 \right)$$

$$= \frac{2}{3} + 2 = \frac{8}{3}$$

8. Find the area of the "triangular" region in the first quadrant that is bounded above by the curve $y = e^{2x}$, below by the curve $y = e^x$, and on the right by the line $x = \ln 3$.



$$\text{Area} = \int_0^{\ln 3} (e^{2x} - e^x) dx$$

$$= \left(\frac{e^{2x}}{2} - e^x \right) \Big|_0^{\ln 3}$$

$$= \left(\frac{9}{2} - 3 \right) - \left(\frac{1}{2} - 1 \right) = 4 - 2 = 2$$