

Name _____

MAT21C Written Assignment
Due Thursday, 8/10

Read, Reflect, and React (or Respond) Prompt #3

In 1994, when I was taking Algebra in high school, my teacher Mrs. N went on a tangent, and we as a class discussed whether $.9999\ldots = 1$. She realized that $.9999\ldots = 0.3333\ldots + 0.3333\ldots + 0.3333\ldots = 1/3 + 1/3 + 1/3 = 1$, but she still didn't believe that $0.9999\ldots = 1$. Her reasoning was the following: $0.999\ldots$ can't equal 1 because in order for equality to occur there eventually needs to be a $0.0000\ldots 1$ added to $0.9999\ldots 9$ in order to make it a 1, and it was a mystery to her where this magical $0.000\ldots 1$ comes from. Show that you can prove and explain why $0.9999\ldots = 1$ by doing the following:

1. Use your knowledge of a geometric series to convert $0.9999\ldots$ into a fraction and prove that $0.9999\ldots = 1$.
2. Provide a counter argument to try and convince my high school teacher that indeed $0.9999\ldots = 1$. Assume she doesn't know Calculus and your argument can't use any Calculus facts or definitions. This is an exercise in trying to explain a complicated math model to someone that doesn't have the necessary math background to truly understand it.