PROBLEM: Consider the two-dimensional graph G of any equation in two variables, i.e., consider G to be a graph in the xy-plane, the yz-plane, or the the xz-plane. Create a surface of revolution in three-dimensional space by revolving G around an axis (line) L. (Line L may be vertical, horizontal, or tilted.) We want to determine an equation for this surface using an arbitrary point (x, y, z) on the surface.

## SOLUTION:

Step 1. Select a random point P = (x, y, z) on the three-dimensional surface. The goal is to use these variables to write an equation which represents this surface.

Step 2. Determine the point Q, which

- a.) depends on point P,
- b.) lies on the axis of revolution L,

and

c.) is nearest point P.

Step 3. Determine the point R, which

- a.) depends on point Q,
- b.) lies on the original graph G,

and so that

- c.) points P, Q, and R are now part of a cross-sectional circle with Q at the center and segments PQ and QR forming radii of the circle.
- Step 4. Use the distance formula to compute the lengths of PQ and QR. The equation can now be determined by setting

$$length PQ = length QR$$

