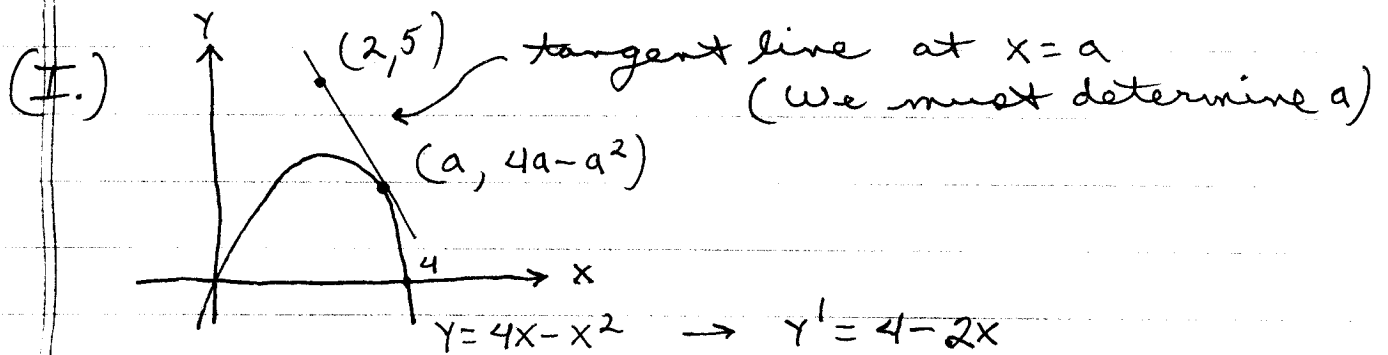


H.W. #8



Slope of tangent line at $x=a$ is

$$4 - 2a = \frac{5 - (4a - a^2)}{2 - a} \rightarrow$$

derivative rise
run

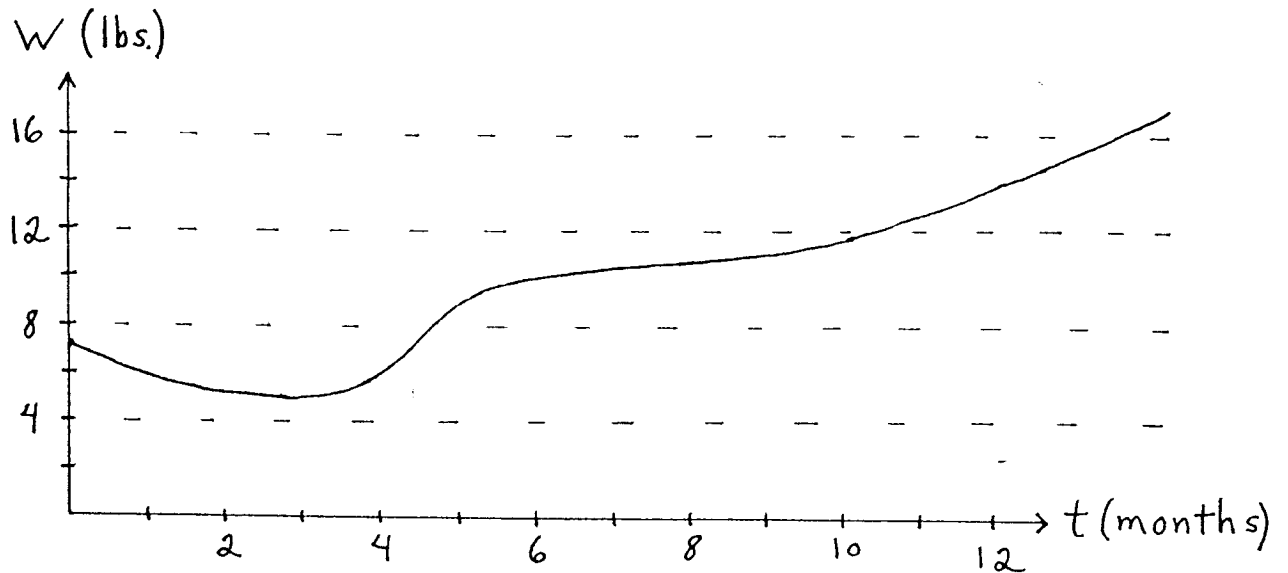
$$8 - 4a - 4a + 2a^2 = 5 - 4a + a^2 \rightarrow a^2 - 4a + 3 = 0 \rightarrow$$

$$(a-1)(a-3) = 0 \rightarrow$$

$$a=1 \rightarrow \text{point } (1, 3) \quad \text{or}$$

$$a=3 \rightarrow \text{point } (3, 3)$$

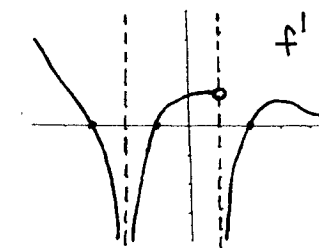
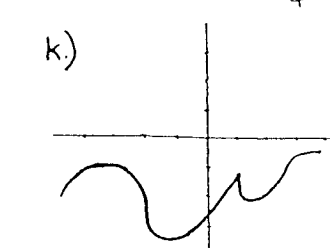
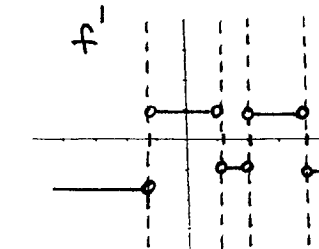
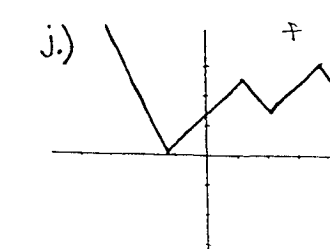
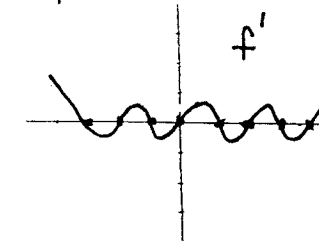
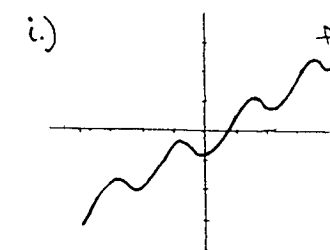
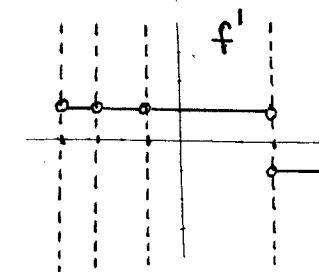
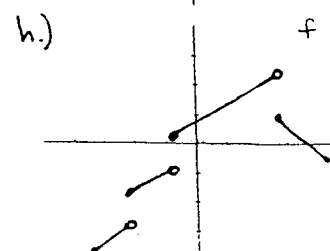
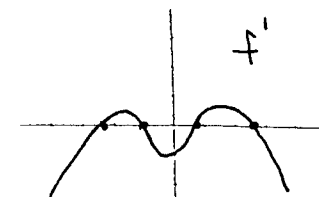
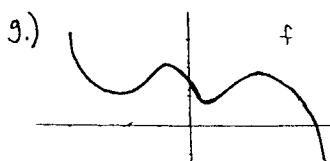
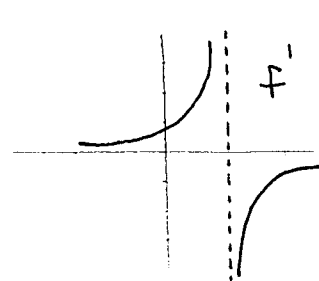
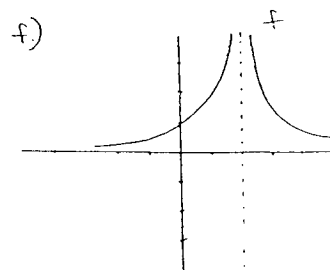
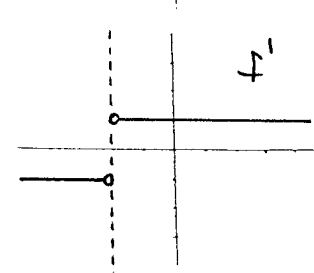
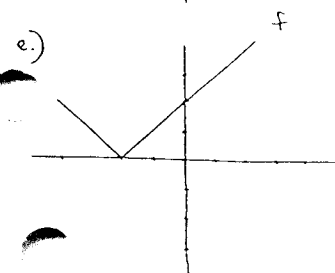
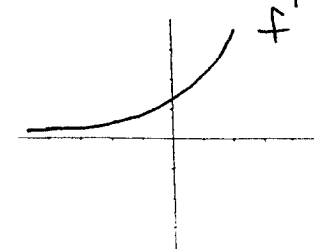
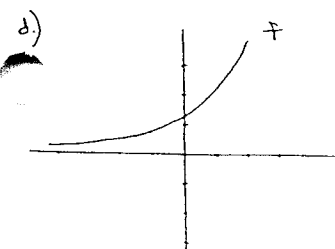
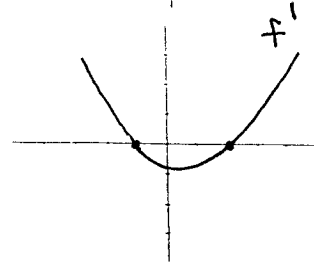
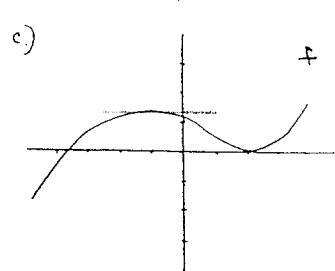
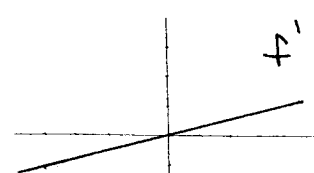
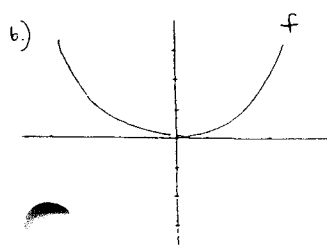
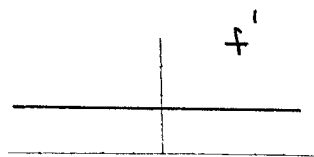
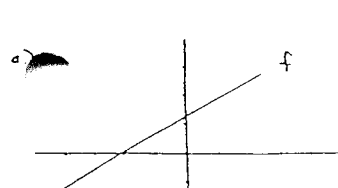
2. The following chart represents the weight W (lbs.) of a newborn baby as a function of time t (months).



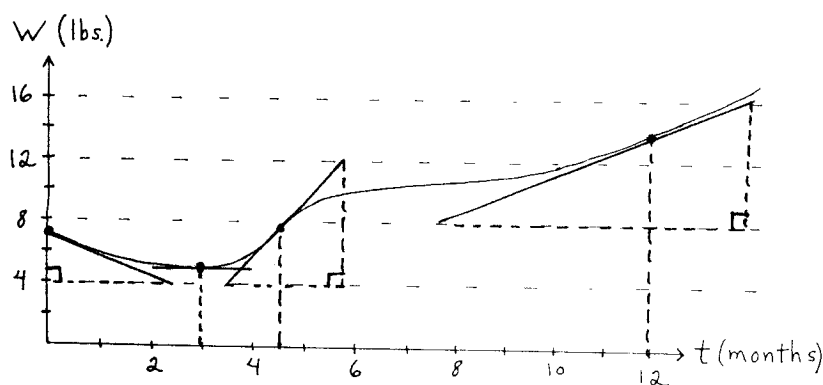
- What is the baby's weight at birth ? after 3 months ? after 1 year ?
- What is an estimate of the baby's growth rate (lbs./month) at birth ? after 3 months ? after 1 year ?
- When is the baby growing at the fastest rate during its first year of life and what is an estimate for this rate ?

Math 16A
Vogler
Worksheet 4

1. Use the given graph of function f to sketch a graph of its derivative, f' .



2.)



a.) $t=0 \rightarrow W=7 \text{ lbs.}$, $t=3 \text{ mo.} \rightarrow W=5 \text{ lbs.}$,
 $t=1 \text{ yr.} \rightarrow W=14 \text{ lbs.}$

b.) growth rate : slope of tangent line
 $t=0 \rightarrow \text{slope} = \frac{-3}{2.5} = -1.2 \text{ lbs./mo.}$,

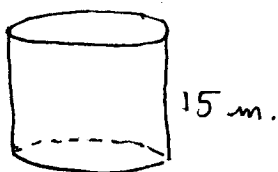
$t=3 \text{ mo.} \rightarrow \text{slope} = 0 \text{ lbs./mo.}$,

$t=1 \text{ yr.} \rightarrow \text{slope} = \frac{8}{6.5} = 1.23 \text{ lbs./mo.}$

c.) The baby is growing at the fastest rate when $t=4\frac{1}{2}$ months. The growth rate is

$$\frac{8}{2.5} = 3.2 \text{ lbs./mo.}$$

SA4:



$$C = 2\pi r \rightarrow 25 = 2\pi r \rightarrow$$

$$r = \frac{25}{2\pi} \text{ m. so volume}$$

$$V = \pi r^2 h = \pi \left(\frac{25}{2\pi}\right)^2 (15) = 746.04 \text{ m}^3 \text{ (ice)}$$

(conversion : $1 \text{ ft}^3 = 0.028 \text{ m}^3$)

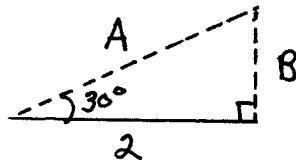
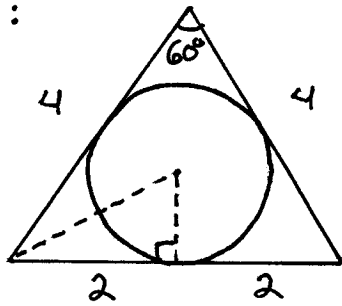
$$V = 26,644.243 \text{ ft}^3 \text{ (ice)}$$

(density ice = 0.917 density water so
 volume water = 0.917 volume ice)

$$V = 24,432.771 \text{ ft}^3 \text{ (water)} ;$$

1 acre = 43,560 ft. so depth of water
 is $\frac{24,432.771 \text{ ft.}^3}{43,560 \text{ ft.}} = 0.56 \text{ ft.} = 6.7 \text{ inches}$

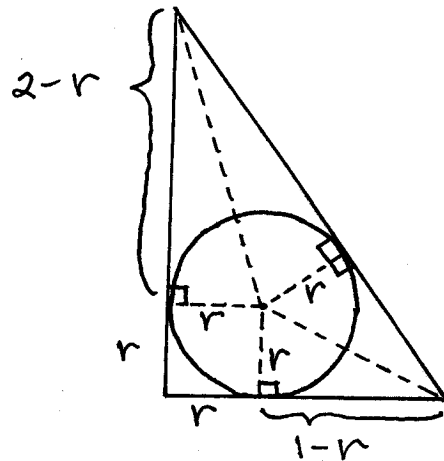
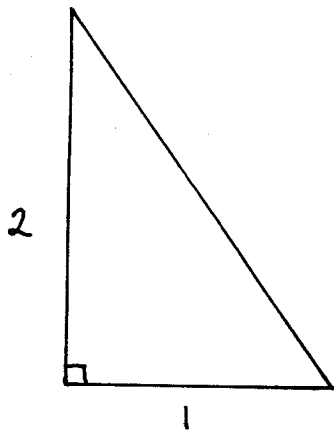
SA7:



a.) $\cos 30^\circ = \frac{2}{A} \rightarrow$
 $A = \frac{2}{\cos 30^\circ} = \frac{2}{\frac{\sqrt{3}}{2}} = \frac{4}{\sqrt{3}} \text{ mi.}$

b.) $\sin 30^\circ = \frac{B}{A} \rightarrow B = A \sin 30^\circ = \frac{4}{\sqrt{3}} \cdot \frac{1}{2} = \frac{2}{\sqrt{3}} \text{ mi.}$

SA9:



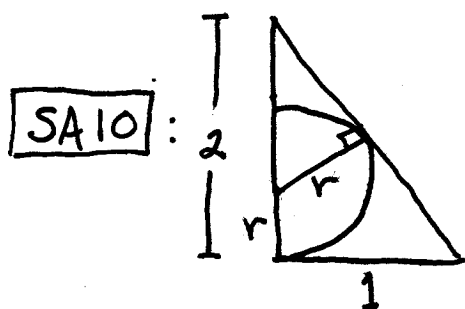
Area large Δ = Areas of 4 small Δ 's
 + Area $\square$

$$\frac{1}{2}(1)(2) = \frac{1}{2}(1-r)r + \frac{1}{2}(1-r)r + \frac{1}{2}(2-r)r + \frac{1}{2}(2-r)r + r^2$$

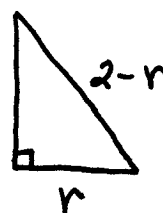
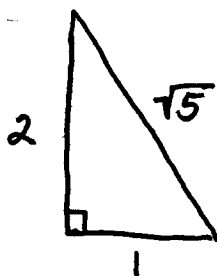
$$\rightarrow 1 = \frac{1}{2}(r-r^2) + \frac{1}{2}(r-r^2) + \frac{1}{2}(2r-r^2) + \frac{1}{2}(2r-r^2) + r^2$$

$$\rightarrow 1 = r - r^2 + 2r - r^2 + r^2 \rightarrow r^2 - 3r + 1 = 0 \rightarrow$$

$$r = \frac{3 \pm \sqrt{9-4}}{2} = \frac{3-\sqrt{5}}{2} \approx 0.38$$



Use similar triangles:



$$\frac{\sqrt{5}}{1} = \frac{2-r}{r} \rightarrow \sqrt{5}r = 2-r \rightarrow r + \sqrt{5}r = 2 \rightarrow (1+\sqrt{5})r = 2 \rightarrow r = \frac{2}{1+\sqrt{5}}$$

SA11: Old K.E. = $\frac{1}{2}mv^2$

a.) New K.E. = $\frac{1}{2}(2m)(3v)^2 = 18(\frac{1}{2}mv^2)$
 $= 18$ (Old K.E.)

b.) New K.E. = $\frac{1}{2}(1.4m)(0.75v)^2$
 $= 0.7875(\frac{1}{2}mv^2) = 0.7875$ (Old K.E.)

so K.E. decreases by $0.2125 = 21.25\%$.

c.) New K.E. = $\frac{1}{2}(0.25m)(2v)^2 = \frac{1}{2}mv^2 = \text{Old K.E.}$

so K.E. remains unchanged.